



Standard 10

MATHEMATICS

Time: 3.00 Hrs.

Marks: 100

I. Choose the best answer:

14×1=14

- 1) If $n(A \times B) = 6$ and $A = \{1, 3\}$ then $n(B)$ is
a) 1 b) 2 c) 3 d) 6
- 2) If $f(x) = x^m$ and $g(x) = x^n$ does $f \circ g = ?$
a) x^m b) x^{m+n} c) x^{mn} d) x^n
- 3) Using Euclid's division lemma, if the cube of any positive integer is divided by 9 then the possible remainders are
a) 0, 1, 8 b) 1, 4, 8 c) 0, 1, 3 d) 1, 3, 5
- 4) The least number that is divisible by all the numbers from 1 to 10 (both inclusive) is
a) 2025 b) 5220 c) 5025 d) 2520
- 5) The value of $(1^3+2^3+3^3+\dots+15^3) - (1+2+3+\dots+15)$ is
a) 14400 b) 14200 c) 14280 d) 14520
- 6) Which of the following should be added to make x^4+64 a perfect square?
a) $4x^2$ b) $16x^2$ c) $8x^2$ d) $-8x^2$
- 7) Graph of a linear equation is a _____.
a) Straight line b) Circle c) Parabola d) None of these
- 8) What is the value of x in $3\sqrt{x} = 9$?
a) 3 b) 9 c) $\sqrt{9}$ d) $\sqrt{3}$
- 9) If $\triangle ABC$, is an isosceles triangle with $\angle C = 90^\circ$ and $AC = 5$ cm, then AB is
a) 2.5 cm b) 5 cm c) 10 cm d) $5\sqrt{2}$ cm
- 10) If in $\triangle ABC$, $DE \parallel BC$. $AB = 3.6$ cm, $AC = 2.4$ cm and $AD = 2.1$ cm then the length of AE is
a) 1.4 cm b) 1.8 cm c) 1.2 cm d) 1.05 cm
- 11) The slope of the line which is perpendicular to a line joining the points $(0, 0)$ and $(-8, 8)$ is
a) -1 b) 1 c) $1/3$ d) -8
- 12) The point of intersection of $x-y = 4$ and $x+y = 8$ is
a) $(2, 6)$ b) $(1, 3)$ c) $(6, 2)$ d) $(4, 8)$
- 13) $\tan\theta \operatorname{cosec}^2\theta - \tan\theta$ is equal to
a) $\sec\theta$ b) $\cot^2\theta$ c) $\sin\theta$ d) $\cot\theta$
- 14) When will the values of $\sin\theta$ and $\cos\theta$ be equal?
a) $\theta = 0^\circ$ b) $\theta = 90^\circ$ c) $\theta = 30^\circ$ d) $\theta = 45^\circ$

II. Answer any 10 questions: [Q.No. 28 is compulsory]

10×2=20

- 15) If $B \times A = \{(-2, 3), (-2, 4), (0, 3), (0, 4), (3, 3), (3, 4)\}$ find A and B .
- 16) A relation $f: X \rightarrow Y$ is defined by $f(x) = x^2 - 2$ where, $X = \{-2, -1, 0, 3\}$ and $Y = R$.
i) List the element of f . ii) Is f a function?
- 17) Let f be a function from R to R defined by $f(x) = 3x - 5$, find the values of a and b given that $(a, 4)$ and $(1, b)$ belong to f .
- 18) Find the 4 digit pin number 'pqrs' of an ATM card such that $p^2 \times q^1 \times r^4 \times s^3 = 3,15,000$.
- 19) Find the 8th term of the G.P. 9, 3, 1,
20) Solve: $2x - 3y = 6$, $x + y = 1$.

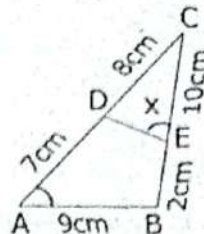
21) Reduce the rational expressions to its lowest form : $\frac{x^2 - 1}{x^2 + x}$

22) Determine the nature of roots for the following quadratic equations:
 $2x^2 - x - 10 = 0$

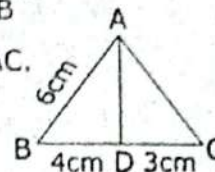
23) Prove the following identities: $\sqrt{\frac{1 + \sin\theta}{1 - \sin\theta}} = \sec\theta + \tan\theta$



- 24) In figure $\angle A = \angle CED$. Prove that $\triangle CAB \sim \triangle CED$. Also find the value of x .



- 25) In the figure AD is the bisector of $\angle BAC$, if $AB = 10$ cm, $AC = 14$ cm and $BC = 6$ cm. Find BD and AC.



- 26) Find the slope of a line joining the points $(5, \sqrt{5})$ with the origin.
 27) Find the equation of a line passing through the point $(3, -4)$ and having slope $-\frac{5}{7}$.
 28) Show that the straight lines $2x+3y-8=0$ and $4x+6y+18=0$ are parallel.

III. Answer any 10 questions: [Q.No. 42 is compulsory]

10×5=50

- 29) A function is defined by $f(x) = 2x-3$
 (i) find $\frac{f(0)+f(1)}{2}$ (ii) find x such that $f(x) = 0$
 (iii) find x such that $f(x) = x$ (iv) find x such that $f(x) = f(1-x)$
 30) Let $f: A \rightarrow B$ be a function defined by $f(x) = \frac{x}{2} - 1$, where $A = \{2, 4, 6, 10, 12\}$, $B = \{0, 1, 2, 4, 5, 9\}$. Represent f by (i) set of ordered pairs (ii) a table (iii) an arrow diagram (iv) a graph.
 31) If $f(x) = 3x-2$, $g(x) = 2x+k$ and if $f \circ g = g \circ f$, then find the value of k .
 32) How many terms of the series $1+5+9+\dots$ must be taken so that their sum is 190?
 33) Find the sum to n terms of the series $3+33+333+\dots$ to n terms.
 34) Rekha has 15 square colour papers of sizes 10 cm, 11 cm, 12 cm, 24 cm. How much area can be decorated with these colour papers?
 35) Solve: $6x+2y-5z = 13$, $3x+3y-2z = 13$, $7x+5y-3z = 26$.
 36) Find the square root of $64x^4-16x^3+17x^2-2x+1$.
 37) If one root of the equation $2y^2-ay+64=0$ is twice the other then find the values of a .
 38) State and prove - Angle Bisector Theorem.
 39) Find the area of the quadrilateral whose vertices are at $(-3, -8)$, $(6, -6)$, $(4, 2)$ and $(-8, 2)$.
 40) If the points $A(2, 2)$, $B(-2, -3)$, $C(1, -3)$ and $D(x, y)$ form a parallelogram then find the value of x and y .
 41) Find the equation of a straight line passing through the points $P(-5, 2)$ and parallel to the line joining the points $Q(3, -2)$ and $R(-5, 4)$.
 42) If $\sin\theta + \cos\theta = \sqrt{3}$ then prove $\tan 3\theta = \frac{3\tan\theta - \tan^3\theta}{1 - 3\tan^2\theta}$.

IV. Answer the following:

2×8=16

- 43) Draw a triangle ABC of base $BC = 8$ cm, $\angle A = 60^\circ$ and the bisector of $\angle A$ meets BC at D such that $BD = 6$ cm. (OR)
 Construct a triangle similar to a given triangle PQR with its sides equal to $\frac{7}{3}$ of the corresponding sides of the triangle PQR (scale factor $\frac{7}{3} > 1$).
 44) Draw the graph of $xy = 24$, $x, y > 0$. Using the graph find, (i) y when $x = 3$ and (ii) x when $y = 6$. (OR)
 A bus is travelling at a uniform speed 50 km/hr. Draw the time-distance graph and hence find
 i) the constant of variation ii) how far will it travel in 90 minutes?
 iii) the time required to cover a distance of 300 km from the graph.